

ELIZADE UN!VERSITY, ILARA-MOKIN, ONDO STATE, NIGERIA

DEPARTMENT OF

MECHANICAL, AUTOMOTIVE AND PRODUCTION **ENGINEERING**

SECOND SEMESTER EXAMINATIONS

2016/2017 ACADEMIC SESSION

COURSE:

GNE 212 – Engineering Mathematics II (3 Units)

CLASS:

200 Level General Engineering

TIME ALLOWED: 3 Hours

INSTRUCTIONS: Answer any five questions

HOD'S SIGNATURE

Date: July/August, 2017

Question 1

Solve the following problem using Euler method (Do - 10 - Steps) (a)

$$y^{I} + y \tan x = \sin 2x, \ y(0) = 1, \ h = 0.1$$

(6marks)

Solve by Gauss Elimination, the system of equations. (b)

$$4x + 2y = 8$$

$$3x + 5y = 6$$

(6marks)

Question 2

Solve the following problem using Euler method (Do - 10 - Steps) (a)

$$y^{I} - xy^{2} = 0$$
, $y(0) = 1$, $h = 0.1$

(6marks)

(b) Find the particular solution of the following equation using the method of undetermined coefficients

$$y^{II} - 2y^I - 3y = 4 + 2x - x^2$$

(6marks)

Question 3

Find the particular solution of the following equation using the method of undetermined coefficients

(a)
$$y^{II} - y^{I} = 2 \sin x$$
, $y_p = A \sin x + B \cos x$

(6marks)

(b) Solve the following ODE

$$(3x^2y^2 + x^2)dx + (2x^3y + y^2)dy = 0 Using Exact Equation (6marks)$$

Question 4

(a) Solve the following ODE

$$\frac{dy}{dx} = \frac{2xy}{x^2 - y^2}$$
 Using Integrating factor. (6marks)

(b) Solve by Gauss Elimination, the system of equations.

$$x - y - z = 0$$
$$3y - 2z = 0$$
$$7x + 2z = 8$$

(6marks)

Question 5

Solve the following by reduction of the 2nd order equation to 1st order equation

(a)
$$y^{II} = 4(y^I)^{3/2}y$$
 (6marks)

(b)
$$x^2y^{II} + (x - x^2)y^I - e^{2x}y = 0$$
 (6marks)

Question 6

Develop the expression for the solution of the following one dimensional wave equation

$$\frac{\partial^2 u}{\partial t^2} = C^2 \frac{\partial^2 u}{\partial x^2} , \quad C = Constant$$
 (12 marks)

Question 7

Solve the following differential equation using method of separation of variables

(a) (i)
$$y' = \frac{x(2 \log(x) + 1)}{\sin y + y \cos y}$$

(4 marks)

(ii)
$$\cos(x+y) dy = dx$$
 (4 marks)

(b) Solve the homogenous equation

$$2xy\frac{dy}{dx} = x^2 + y^2 \qquad \text{(given y=0 at x=1)}$$